

MATHEMATICS

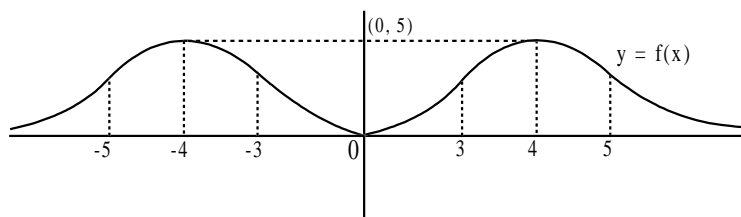
61. If $e^x + e^{f(x)} = e$, then for $f(x)$
- (a) $D_f = (-\infty, 0], R_f = (-\infty, 0]$ (b) $D_f = (-\infty, 1), R_f = (-\infty, 1)$
 (c) $D_f = (-\infty, 0), R_f = (-\infty, 1)$ (d) $D_f = (-\infty, 1], R_f = (-\infty, 1]$
62. If $f(x) = ax^2 + bx + c$ and roots of $f(x) = 0$, represents the slope of two different line. If one of the line is $x + 1 = 0$, then equation of other line passing through origin is.
- (a) $y = (a - b + c)x$ (b) $bx + cy = 0$ (c) $cx + by = 0$ (d) None of these
63. If three vectors $\vec{a}, \vec{b}, \vec{c}$ are such that $\vec{a} \neq \vec{0}$ and $\vec{a} \times \vec{b} = 2\vec{a} \times \vec{c}, |\vec{a}| = |\vec{c}| = 1, |\vec{b}| = 4$ and the angle between \vec{b} and \vec{c} is $\cos^{-1} \frac{1}{4}$ then $\vec{b} - 2\vec{c} = \lambda\vec{a}$ where λ is equal to
- (a) ± 2 (b) ± 4 (c) $\frac{1}{2}$ (d) $\frac{1}{4}$
64. If $I = \int_0^{\pi/2} \ln(\sin x) dx$ then $\int_{-\pi/4}^{\pi/4} \ln(\sin x + \cos x) dx =$
- (a) $\frac{I}{2}$ (b) $\frac{I}{4}$ (c) $\frac{I}{\sqrt{2}}$ (d) I
65. Let z_1, z_2, z_3 be three distinct complex numbers satisfying $|z_1 - 1| = |z_2 - 1| = |z_3 - 1|$. If $z_1 + z_2 + z_3 = 3$ then z_1, z_2, z_3 must represent the vertices of :
- (a) an equilateral triangle (b) an isosceles triangle which is not equilateral
 (c) a right triangle (d) nothing definite can be said
66. If $f(x) = \begin{cases} \sin x, & x \neq n\pi, \\ 2 & \text{otherwise} \end{cases}$ n is an integer $g(x) = \begin{cases} x^2 + 1 & x \neq 0, 2 \\ 4, & x = 0 \\ 5, & x = 2 \end{cases}$ then $\lim_{x \rightarrow 0} g(f(x))$ is
- (a) 1 (b) 5 (c) 6 (d) 7.
67. In a class tournament where the participants were to play one game with another, two class players fell ill, having played 3 games each. If the total number of games played is 84, the number of participants at the beginning was :
- (a) 15 (b) 16 (c) 20 (d) 21
68. The ratio in which the plane $\vec{r} \cdot (\vec{i} - 2\vec{j} + 3\vec{k}) = 17$ divides the line joining the points $-2\vec{i} + 4\vec{j} + 7\vec{k}$ and $3\vec{i} - 5\vec{j} + 8\vec{k}$ is
- (a) 1 : 5 (b) 1 : 10 (c) 3 : 5 (d) 3 : 10
69. The equation to the circle which has a tangent $2x - y - 1 = 0$ at $(3, 5)$ on it and with the centre on $x + y = 5$, is
- (a) $x^2 + y^2 + 6x - 16y + 28 = 0$ (b) $x^2 + y^2 - 6x + 16y - 28 = 0$
 (c) $x^2 + y^2 + 6x + 6y - 28 = 0$ (d) $x^2 + y^2 - 6x - 6y - 28 = 0$

70. Let $f(x) = [x] + |1 - x|$ for $-1 < x < 3$ ($[\]$ denotes the greatest integer function). The point(s), if any where this function is not differentiable, is :
- (a) $\{0, 1\}$ (b) $\{-1, 0\}$ (c) $\{-2\}$ (d) $\{3\}$
71. The vector equation of the plane through the point $(2, 1, -1)$ and passing through the line of intersection of the plane $\vec{r} \cdot (\hat{i} + 3\hat{j} - \hat{k}) = 0$ and $\vec{r} \cdot (\hat{j} + 2\hat{k}) = 0$ is
- (a) $\vec{r} \cdot (\hat{i} + 9\hat{j} + 11\hat{k}) = 0$ (b) $\vec{r} \cdot (\hat{i} + 9\hat{j} + 11\hat{k}) = 6$
 (c) $\vec{r} \cdot (\hat{i} - 3\hat{j} - 13\hat{k}) = 0$ (d) None
72. Solution of the equation $\cos^2 x \frac{dy}{dx} - (\tan 2x)y = \cos^4 x$, $|x| < \frac{\pi}{4}$, when $y\left(\frac{\pi}{6}\right) = \frac{3\sqrt{3}}{8}$ is
- (a) $y = \tan 2x \cos^2 x$ (b) $y = \cot 2x \cdot \cos^2 x$ (c) $y = \frac{1}{2} \tan 2x \cos^2 x$ (d) $y = \frac{1}{2} \cot 2x \cdot \cos^2 x$
73. A tangent and a normal is drawn at the point $P \equiv (16, 16)$ of the parabola $y^2 = 16x$ which cut the axis of the parabola at the points A and B respectively. If the centre of the circle through P, A and B is C then the angle between PC and the axis of x is
- (a) $\tan^{-1} \frac{1}{2}$ (b) $\tan^{-1} 2$ (c) $\tan^{-1} \frac{3}{4}$ (d) $\tan^{-1} \frac{4}{3}$
74. If the equations $x^3 + 5x^2 + px + q = 0$ and $x^3 + 7x^2 + px + r = 0$ have two roots in common, the product of non common roots of two equations is
- (a) 35 (b) -35 (c) $35 + p - q$ (d) $35 + p + q - r$
75. Let $f(x) = \int_0^x (\sin t - \cos t)(e^t - 2)(t - 1)^3 (t - 2)^5 dt$ ($0 < x \leq 4$). Then number of points, where $f(x)$ assumes local maximum value, is
- (a) one (b) two (c) three (d) None of these
76. One hundred identical coins, each with probability, p , of showing up heads are tossed once. If $0 < p < 1$ and the probability of head showing on 50 coins is equal to that of heads showing on 51 coins, then the values of p is
- (a) $\frac{1}{2}$ (b) $\frac{49}{101}$ (c) $\frac{50}{101}$ (d) $\frac{51}{101}$
77. The value of the definite integral $\int_0^1 dx / (x^2 + 2x \cos \alpha + 1)$ for $0 < \alpha < \pi$, is equal to
- (a) $\sin \alpha$ (b) $\tan^{-1} (\sin \alpha)$ (c) $\alpha \sin \alpha$ (d) $(\alpha/2) (\sin \alpha)^{-1}$
78. The slope of the tangent to a curve $y = f(x)$ at $(x, f(x))$ is $2x + 1$. If the curve passes through the point $(1, 2)$, then the area of the region bounded by the curve, the x-axis and the line $x = 1$ is
- (a) $5/6$ (b) $6/5$ (c) $1/6$ (d) 6

79. If $f(x) = x(x-2)(x-4)$, $1 \leq x \leq 4$, then a number satisfying the conditions of the mean value theorem is
 (a) 1 (b) 2 (c) $5/2$ (d) $7/2$
80. If a function $f(x)$ is defined as $f(x) = \min\{1 - \tan^n x, 1 - \sin^n x, 1 - x^n\}$. Then the left derivative of the function at $x = \frac{\pi}{4}$ is;
 (a) $-2n$ (b) $-2(n+1)$ (c) $-n\left(\frac{\pi}{4}\right)^{n-1}$ (d) None of these

Directions for questions 81 to 85.

If any function of $y = f(x)$ is defined as $f: \mathbb{R} \rightarrow [0, 5]$ (See the graph)



81. Which is the wrong statement
 (a) $f(x)$ is having two maxima & one min (b) $f(x)$ is an even function
 (c) curve $y = f(x)$ is having asymptotes (d) all above are wrong
82. $f(x) = (x - 4)^2$ having
 (a) 1 real root (b) 2 real roots (c) 3 real roots (d) no real roots
83. $y = f^{-1}(x)$ can be define for
 (a) $x \in \mathbb{R}$ (b) $x \in (0, 4)$ (c) $x \in (-4, 4)$ (d) $x \in \phi$
84. No. of points of inflection of $y = f(x)$
 (a) 0 (b) 1 (c) 2 (d) 4
85. $\sin^{-1}\left(\frac{f(x)}{5}\right)$ is define for
 (a) $x \in \mathbb{R}$ (b) $x \in \phi$ (c) only for $x \in [-3, 3]$ (d) only for $x \in [-5, 5]$

Directions for questions 86 to 90.

Mr. "A" & "B" solved the following question asked in a question paper

$$\lim_{x \rightarrow \frac{\pi}{2}} \frac{2^{\cot x} - 2^{\cos x}}{\cot x - \cos x}$$

Mr. "A" solved question in following way

$$\lim_{x \rightarrow \frac{\pi}{2}} \frac{2^{\cot x} - 1 + 1 - 2^{\cos x}}{\cot x - \cos x} \dots\dots\dots (\text{step - 1})$$

$$\lim_{x \rightarrow \frac{\pi}{2}} \frac{\frac{2^{\cot x} - 1}{\cot x} \cot x - \frac{2^{\cos x} - 1}{\cos x} \cos x}{\cot x - \operatorname{cosec} x} \dots\dots\dots (\text{step - 2})$$

$$\lim_{x \rightarrow \frac{\pi}{2}} \frac{\cot x (\ln 2) - \cos x (\ln 2)}{\cot x - \cos x} \dots\dots\dots (\text{step - 3})$$

$$\lim_{x \rightarrow \frac{\pi}{2}} \ln 2 \left(\frac{\cot x - \cos x}{\cot x - \cos x} \right) = \ln 2 \text{ Ans} \dots\dots\dots (\text{step - 4})$$

Mr. "B" solved question in following

$$\lim_{x \rightarrow \frac{\pi}{2}} \frac{2^{\cos x} (2^{\cot x - \cos x} - 1)}{\cot x - \cos x} \dots\dots\dots (\text{step - 1})$$

$$= 2^0 \ln 2 \dots\dots\dots (\text{step - 2})$$

$$= \ln 2 \text{ Ans} \dots\dots\dots (\text{step - 3})$$

86. Which is correct statement
 (a) Mr. A gave correct solution but, Mr. B gave wrong solution
 (b) Mr. A gave wrong solution but, Mr. B gave correct solution
 (c) Mr. A & B both gave correct solution.
 (d) Both gave wrong solution
87. Which is correct statement
 (a) Mr. "A" did mistake in (step - 2) (b) Mr. "A" did mistake in (step - 3)
 (c) Mr. "A" did mistake in (step - 4) (d) No mistake in solution given by Mr. "A".
88. Which is correct statement
 (a) Mr. "B" did mistake in (step - 1) (b) Mr. "B" did mistake in (step - 2)
 (c) Mr. "B" did mistake in (step - 3) (d) No mistake in solution given by Mr. "B".
89. Mr. "A" did mistake because
 (a) In (step - 2) he multiply by $\cot x$ & $\cos x$ in N^r & D^r which is zero.
 (b) In (step - 3) he solved the limit partially
 (c) In (step - 4) he cancelled the term $(\cot x - \cos x)$ which is zero for $x = \frac{\pi}{2}$
 (d) No mistake in any step.
90. Mr. "B" did mistake because
 (a) he took $2^{\cos x}$ common in (step - 1)
 (b) he considered that $\lim_{x \rightarrow \frac{\pi}{2}} \frac{2^{\cot x - \cos x} - 1}{\cot x - \cos x}$ is same as $\lim_{x \rightarrow 0} \frac{2^x - 1}{x}$
 (c) In step - 3 he kept $2^{\cos x}$ as 2^0
 (d) no mistake in solution given by Mr. B.

IITian Test Series

2006 BATCH



Student's Name :

Q.No	A	B	C	D	Q.No	A	B	C	D	Q.No	A	B	C	D
1.	O	O	O	O	31.	O	O	O	O	61.	O	O	O	O
2.	O	O	O	O	32.	O	O	O	O	62.	O	O	O	O
3.	O	O	O	O	33.	O	O	O	O	63.	O	O	O	O
4.	O	O	O	O	34.	O	O	O	O	64.	O	O	O	O
5.	O	O	O	O	35.	O	O	O	O	65.	O	O	O	O
6.	O	O	O	O	36.	O	O	O	O	66.	O	O	O	O
7.	O	O	O	O	37.	O	O	O	O	67.	O	O	O	O
8.	O	O	O	O	38.	O	O	O	O	68.	O	O	O	O
9.	O	O	O	O	39.	O	O	O	O	69.	O	O	O	O
10.	O	O	O	O	40.	O	O	O	O	70.	O	O	O	O
11.	O	O	O	O	41.	O	O	O	O	71.	O	O	O	O
12.	O	O	O	O	42.	O	O	O	O	72.	O	O	O	O
13.	O	O	O	O	43.	O	O	O	O	73.	O	O	O	O
14.	O	O	O	O	44.	O	O	O	O	74.	O	O	O	O
15.	O	O	O	O	45.	O	O	O	O	75.	O	O	O	O
16.	O	O	O	O	46.	O	O	O	O	76.	O	O	O	O
17.	O	O	O	O	47.	O	O	O	O	77.	O	O	O	O
18.	O	O	O	O	48.	O	O	O	O	78.	O	O	O	O
19.	O	O	O	O	49.	O	O	O	O	79.	O	O	O	O
20.	O	O	O	O	50.	O	O	O	O	80.	O	O	O	O
21.	O	O	O	O	51.	O	O	O	O	81.	O	O	O	O
22.	O	O	O	O	52.	O	O	O	O	82.	O	O	O	O
23.	O	O	O	O	53.	O	O	O	O	83.	O	O	O	O
24.	O	O	O	O	54.	O	O	O	O	84.	O	O	O	O
25.	O	O	O	O	55.	O	O	O	O	85.	O	O	O	O
26.	O	O	O	O	56.	O	O	O	O	86.	O	O	O	O
27.	O	O	O	O	57.	O	O	O	O	87.	O	O	O	O
28.	O	O	O	O	58.	O	O	O	O	88.	O	O	O	O
29.	O	O	O	O	59.	O	O	O	O	89.	O	O	O	O
30.	O	O	O	O	60.	O	O	O	O	90.	O	O	O	O

NOTE : USE ONLY HB PENCIL. USAGE OF PENS WILL INVITE DISQUALIFICATION.